

Table 1- Submissions for KCS resistance test and seakeeping in calm water and head waves at $Fr=0.26$

No	Institute	Code	Turbulence	Free Surface	Discretization	Grid motion	Grid type	Grid size	No .CPU	CPU Time
1	FORCE	StarCCM ⁺	k- ϵ /k- ω SST	VOF	Finite Vol.	Dynamic Overset	Unstructured	18 -28 M	NA	NA
2	HSVA	FreSCo ⁺	k- ϵ /k- ω	VOF	Finite Vol.	Dynamic	Unstructured	NA	NA	NA
3	IIHR	CFDShip-Iowa V4.5	k- ϵ /k- ω SST	LS Single Ph.	Finite Dif.	Dynamic Overset	Structured	29.2 M	224	16128 CPUh
4	KRISO	WAVIS	k- ϵ /k- ω EARSM	LS	Finite Vol.	Dynamic	Structured	10 M Half B.	38	170.3 CPUh
5	MARIC	FINEMarine	k- ϵ /k- ω SST	VOF	Finite Vol.	Deforming	Unstructured	1.18-6.9M	NA	NA
6	NMRI	NAGISA	k- ϵ /k- ω EARSM	LS	Finite Vol.	Deforming	Unstructured	4.4 M	2	250 CPUh
7	NUMECA	ISISCFD	k- ϵ /k- ω SST	VOF	Finite Vol.	Deforming, Overset	Unstructured	2M Half B.	NA	3116 CPUh
8	UDE	OpenFOAM	k- ϵ /k- ω SST	VOF	Finite Vol.	Deforming	Unstructured	1.06 M	8	104 CPUh
9	UM	OF23x	k- ϵ /k- ω SST	VOF	Finite Vol.	Dynamic	Unstructured	2.6 M	48	3800 CPUh
10	UNIZAG-FSB	swenseFoam	k- ϵ /k- ω SST	LS	Finite Vol.	Dynamic	Unstructured	0.61-1.6 M	40	817 CPUh
Ave.								9.80 M	60	3484
G2010 (6 sub.)								2.62 M (0.55-7.6 M)		

Table 2- Mean and SD of submission values for KCS calm water resistance at $Fr=0.26$

	$C_T \times 10^3$	Sinkage/ L_{pp}	Trim (deg)
\bar{S}	3.8500	-0.0019	-0.1686
SD% \bar{S}	2.67	2.93	5.36

Table 3- Mean and SD of submission values for 0th amplitude of motions and resistance for KCS seakeeping at $Fr=0.26$

	Cases	$C_T \times 10^3$	AR	Heave/A	Pitch/Ak	Ave.
\bar{S}	$\lambda/L=0.65$	8.488	4.488	-0.738	-0.107	
	$\lambda/L=0.85$	9.508	6.666	-0.575	-0.131	
	$\lambda/L=1.15$	14.783	10.723	-0.267	-0.007	
	$\lambda/L=1.37$	14.512	7.030	-0.324	-0.020	
	$\lambda/L=1.95$	11.198	2.103	-0.188	-0.058	
SD% \bar{S}	$\lambda/L=0.65$	6.20	49.31	10.79	13.85	20.04
	$\lambda/L=0.85$	5.15	24.70	11.59	86.01	31.86
	$\lambda/L=1.15$	10.11	20.14	23.04	228.66	70.49
	$\lambda/L=1.37$	11.62	24.52	102.38	114.81	63.33
	$\lambda/L=1.95$	6.87	24.14	14.27	21.55	16.71
	Ave.	7.99	28.56	32.41	92.98	40.49

Table 4- Mean and SD of submission values for 1st harmonic amplitudes and phases for KCS seakeeping at Fr=0.26

		ζ/L	$C_T \times 10^3$		Heave/A		Pitch/Ak		Ave.	
	Cases	Amp	Amp	Phase	Amp	Phase	Amp	Phase	Amp	Phase
\bar{S}	$\lambda/L=0.65$	0.005	2.743	-0.992	0.117	1.129	0.011	0.858		
	$\lambda/L=0.85$	0.006	3.997	-0.760	0.215	1.109	0.218	2.028		
	$\lambda/L=1.15$	0.010	3.126	-1.573	0.889	1.068	0.705	-2.591		
	$\lambda/L=1.37$	0.012	10.856	-1.240	0.884	-2.348	0.906	-1.631		
	$\lambda/L=1.95$	0.016	22.094	-0.324	0.892	-1.716	1.062	-0.585		
SD% \bar{S}	$\lambda/L=0.65$	2.30	13.68	5.64	12.19	107.86	83.44	41.59	27.90	51.69
	$\lambda/L=0.85$	1.77	9.50	35.33	23.23	133.23	17.93	8.08	13.10	58.88
	$\lambda/L=1.15$	2.22	5.47	20.58	11.55	253.86	9.60	5.56	7.21	93.33
	$\lambda/L=1.37$	2.83	18.48	12.99	8.53	4.64	10.19	8.99	10.01	8.87
	$\lambda/L=1.95$	2.10	7.67	53.79	6.18	11.24	6.62	28.96	5.64	31.33
	Ave.	2.25	10.96	25.67	12.33	102.17	25.55	18.63	12.77	48.82

Table 5- Mean and SD of submission values for 2nd harmonic amplitudes and phases for KCS seakeeping at Fr=0.26

		$C_T \times 10^3$		Heave/A		Pitch/Ak		Ave.	
	Cases	Amp	Phase	Amp	Phase	Amp	Phase	Amp	Phase
\bar{S}	$\lambda/L=0.65$	0.286	-0.564	0.003	2.022	0.002	2.119		
	$\lambda/L=0.85$	0.568	-0.753	0.007	-1.823	0.004	-1.259		
	$\lambda/L=1.15$	2.580	0.289	0.015	-0.184	0.014	0.289		
	$\lambda/L=1.37$	2.074	0.109	0.105	0.551	0.015	0.623		
	$\lambda/L=1.95$	0.892	-0.668	0.019	1.053	0.036	1.279		
SD% \bar{S}	$\lambda/L=0.65$	40.74	103.80	103.85	62.30	86.53	24.61	77.04	63.57
	$\lambda/L=0.85$	23.69	166.25	38.42	104.90	65.64	175.48	42.59	148.88
	$\lambda/L=1.15$	25.49	570.03	37.06	321.03	15.68	336.35	26.07	409.14
	$\lambda/L=1.37$	37.92	3974.68	263.14	129.64	57.58	56.56	119.6	1387.0
	$\lambda/L=1.95$	48.45	156.46	10.61	45.14	21.94	117.07	27.00	106.23
	Ave.	35.26	994.24	90.62	132.60	49.47	142.02	58.45	422.95

Table 6- Comparison error for KCS calm water resistance test submissions at Fr=0.26

No	Institute	Code	$C_T \times 10^3$	Sinkage/ L_{pp}	Trim (deg)	Ave.
	<i>FORCE</i>	<i>Experiment</i>	<i>3.835⁺</i>	<i>-2.074E-03</i>	<i>-0.1646</i>	
1	FORCE	StarCCM ⁺	2.45	13.06	4.39	6.63
2	HSVA	FreSCo ⁺	-3.13	4.42	2.48	3.34
3	IIHR	CFDShip-Iowa	-0.26	9.43	-9.21	6.30
4	KRISO	WAVIS	2.53	4.73	-4.83	4.03
5	MARIC	FINEMarine31_3	-0.02	-0.20	-15.60	3.17
6	NMRI	NAGISA	-3.86	5.84	0.11	3.27
7	NUMECA	ISISCFD	-1.64	5.98	-3.17	3.60
8	UDE	OpenFOAM	2.74			2.74
9	UM	OF23x	2.01	8.18	-10.58	6.92
10	UNIZAG-FSB	swenseFoam	-4.70	8.06	-6.59	6.45
<u>Based on Actual Errors</u>						
Ave E%D*			-0.39	7.11	-2.46	<u>3.32</u>
SD E%D			2.68	2.72	5.49	<u>3.63</u>
G2010 Ave E%D at Fr=0.26 (All Fr)⁺⁺			-2.55 (-2.02)	3.67 (-20.31)	-0.24 (-10.87)	<u>2.15 (11.06)</u>
G2010 SD E%D at Fr=0.26 (All Fr)			3.25 (3.46)	2.20 (6.10)	3.93 (9.11)	<u>3.12 (6.22)</u>
G2010 Ave E%D for Fr>0.2 (Fr<0.2)			-2.37 (-1.42)	0.18 (-40.80)	0.80 (-22.52)	<u>1.16 (21.58)</u>
G2010 SD E%D for Fr>0.2 (Fr<0.2)			3.21 (3.80)	2.65 (9.54)	4.38 (13.84)	<u>3.41 (9.06)</u>
<u>Based on Absolute Errors</u>						
Ave E %D			2.33	7.11	5.18	<u>4.87</u>
SD E %D			1.38	2.72	3.08	<u>2.39</u>
G2010 Ave E %D at Fr=0.26 (All Fr)⁺⁺			3.03 (3.25)	4.33 (22.34)	3.46 (15.98)	<u>3.61 (13.86)</u>
G2010 SD E %D at Fr=0.26 (All Fr)			2.83 (2.64)	1.46 (5.80)	2.34 (7.37)	<u>2.21 (5.27)</u>
G2010 Ave E %D for Fr>0.2 (Fr<0.2)			3.11 (3.36)	3.88 (40.80)	4.82 (27.14)	<u>3.94 (23.77)</u>
G2010 SD E %D for Fr>0.2 (Fr<0.2)			2.87 (2.51)	2.05 (9.54)	2.72 (12.03)	<u>2.54 (8.03)</u>

* $E\%D = 100 \times (D - S)/D$ where D and S are data and simulation values.

⁺ Resistance coefficient is based on wetted surface area (S/L^2) = 0.1818 with rudder in calm water

⁺⁺ Case 2.2b reported in Chapter 2 for KCS calm water resistance with free to sinkage and trim (6 submissions)

Table 7- Comparison error for 0th harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.65$

No	Institute	Code	$C_{T0} \times 10^3$	AR	z_0/A	θ_0/Ak	Ave.
	<i>FORCE</i>	<i>Experiment</i>	8.237	3.386	-0.8097	-0.1079	
1	FORCE	StarCCM ⁺	3.89	23.32	13.43	5.96	11.65
2	HSVA	FreSCo ⁺	-4.13	-17.75	5.03	-3.67	7.65
3	IIHR	CFDShip-Iowa V4.5	-1.87	-23.65	9.01	-5.23	9.94
4	KRISO	WAVIS	1.30	-15.42	6.33	-0.94	5.99
5	MARIC	FINEMarine31_3	0.33	5.05	13.05	34.21	13.16
6	NMRI	NAGISA	-14.00	-151.31	2.33	-16.38	46.00
7	NUMECA	ISISCFD	0.47	28.99	6.94	-5.50	10.48
8	UDE	OpenFOAM	-2.93	-20.36	32.56		18.62
9	UM	OF23x	2.42	7.99	8.17	-10.89	7.37
10	UNIZAG	swenseFoam	-15.91	-167.65	-8.47	6.89	49.73
Ave E%D			-3.04	-33.08	8.84	0.49	11.36
SD E%D			6.39	65.62	9.84	13.78	23.91
Ave E %D			4.72	46.15	10.53	9.96	17.84
SD E %D			5.27	57.19	8.00	9.54	20.00

Table 8- Comparison error for 0th harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.85$

No	Institute	Code	$C_{T0} \times 10^3$	AR	z_0/A	θ_0/Ak	Ave.
	<i>FORCE</i>	<i>Experiment</i>	9.269	6.102	-0.6279	-0.1302	
1	FORCE	StarCCM ⁺					
2	HSVA	FreSCo ⁺	-1.51	6.21	6.34	26.08	10.04
3	IIHR	CFDShip-Iowa V4.5	-8.19	-46.26	14.10	33.75	25.58
4	KRISO	WAVIS	-3.01	-29.59	8.05	35.51	19.04
5	MARIC	FINEMarine31_3	3.71	21.58	10.34	41.64	19.32
6	NMRI	NAGISA	-8.99	-33.63	3.77	19.53	16.48
7	NUMECA	ISISCFD	0.52	10.86	8.76	26.28	11.60
8	UDE	OpenFOAM	3.64	28.96	27.06	-245.54	76.30
9	UM	OF23x	1.70	0.21	12.59	23.67	9.54
10	UNIZAG	swenseFoam	-11.01	-41.26	-15.82	31.45	24.88
Ave E%D			-2.57	-9.21	8.35	-0.85	5.25
SD E%D			5.28	26.97	10.62	86.74	32.40
Ave E %D			4.70	24.29	11.87	53.72	23.64
SD E %D			3.53	14.92	6.45	68.11	23.25

Table 9- Comparison error for 0th harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.15$

No	Institute	Code	$C_{T0} \times 10^3$	AR	z_0/A	θ_0/Ak	Ave.
	<i>FORCE</i>	<i>Experiment</i>	14.164	9.911	-0.2779	-0.0022	
1	FORCE	StarCCM ⁺	1.39	0.13	10.48	445.93	114.48
2	HSVA	FreSCo ⁺	-1.59	0.22	2.78	57.51	15.53
3	IIHR	CFDShip-Iowa V4.5	-26.83	-58.22	17.92	253.38	89.09
4	KRISO	WAVIS	14.41	28.45	15.47	-2157.21	553.88
5	MARIC	FINEMarine31_3	1.61	3.53	19.41	-549.83	143.59
6	NMRI	NAGISA	-16.91	-32.32	-15.39	-178.50	60.78
7	NUMECA	ISISCFD	-1.85	-2.09	11.39	237.67	63.25
8	UDE	OpenFOAM	-2.38	-3.25	21.21		8.94
9	UM	OF23x	-3.77	-10.59	12.56	36.30	15.81
10	UNIZAG	swenseFoam	-7.89	-11.54	-54.96	-145.99	55.09
Ave E%D			-4.38	-8.57	4.09	-222.30	59.83
SD E%D			10.56	21.87	22.10	736.99	197.88
Ave E %D			7.86	15.03	18.16	451.37	123.10
SD E %D			8.29	18.04	13.24	623.57	165.79

Table 10- Comparison error for 0th harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.37$

No	Institute	Code	$C_{T0} \times 10^3$	AR	z_0/A	θ_0/Ak	Ave.
	<i>FORCE</i>	<i>Experiment</i>	13.948	6.512	-0.2491	-0.0075	
1	FORCE	StarCCM ⁺	-0.37	-3.82	19.15	124.81	37.04
2	HSVA	FreSCo ⁺	-4.78	-6.80	13.24	26.43	12.81
3	IIHR	CFDShip-Iowa V4.5	-22.81	-50.38	19.62	-75.67	42.12
4	KRISO	WAVIS	17.74	36.32	72.73	-909.06	258.96
5	MARIC	FINEMarine31_3	-13.73	-30.47	-399.50	-220.97	166.17
6	NMRI	NAGISA	12.36	32.18	5.20	-377.45	106.80
7	NUMECA	ISISCFD	-3.50	-5.77	18.62	112.14	35.01
8	UDE	OpenFOAM					
9	UM	OF23x	-7.18	-18.42	19.42	44.07	22.27
10	UNIZAG	swenseFoam	-14.13	-25.66	-40.55	-243.25	80.90
Ave E%D			-4.04	-8.09	-30.23	-168.77	52.78
SD E%D			12.09	26.51	133.33	308.58	120.13
Ave E %D			10.73	23.31	67.56	237.09	84.67
SD E %D			6.88	14.99	118.85	259.80	100.13

Table 11- Comparison error for 0th harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.95$

No	Institute	Code	$C_{T0} \times 10^3$	AR	z_0/A	θ_0/Ak	Ave.
	<i>FORCE</i>	<i>Experiment</i>	10.798	1.909	-0.2004	-0.0571	
1	FORCE	StarCCM ⁺	4.09	8.13	8.96	-0.55	5.43
2	HSVA	FreSCo ⁺	-1.93	1.00	4.05	-5.44	3.11
3	IIHR	CFDShip-Iowa V4.5	-14.39	-49.07	13.46	-10.27	21.80
4	KRISO	WAVIS	1.98	0.63	19.26	-34.20	14.02
5	MARIC	FINEMarine31_3	-16.75	-64.04	14.18	47.42	35.60
6	NMRI	NAGISA	2.85	19.29	8.09	-23.56	13.45
7	NUMECA	ISISCFD	3.14	14.86	23.35	-11.10	13.11
8	UDE	OpenFOAM	-1.45	-0.98	-9.77		4.07
9	UM	OF23x	-9.02	-36.07	2.64	0.38	12.02
10	UNIZAG	swenseFoam	-5.57	-7.70	-24.37	14.74	13.09
Ave E%D			-3.70	-11.40	5.99	-2.51	5.90
SD E%D			7.12	26.89	13.41	22.09	17.38
Ave E %D			6.12	20.18	12.81	16.41	13.88
SD E %D			5.20	21.12	7.18	15.01	12.13

Table 12- Average comparison error $E\%D$ for 0th harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	C_{T0}	AR	z_0/A	θ_0/Ak	Ave $E\%D$
1	FORCE	StarCCM ⁺	2.25	6.94	13.01	144.04	41.56
2	HSVA	FreSCo ⁺	-2.79	-3.42	6.29	20.18	8.17
3	IIHR	CFDShip-Iowa V4.5	-14.82	-45.52	14.82	39.19	28.59
4	KRISO	WAVIS	6.48	4.08	24.37	-613.18	162.03
5	MARIC	FINEMarine31_3	-4.97	-12.87	-68.50	-129.51	53.96
6	NMRI	NAGISA	-4.94	-33.16	0.80	-115.27	38.54
7	NUMECA	ISISCFD	-0.24	9.37	13.81	71.90	23.83
8	UDE	OpenFOAM	-0.78	1.09	17.77	-245.54	66.29
9	UM	OF23x	-3.17	-11.37	11.08	18.71	11.08
10	UNIZAG	swenseFoam	-10.90	-50.76	-28.83	-67.23	39.43
Ave $E\%D$			-3.39	-13.56	0.46	-87.67	26.27
SD $E\%D$			5.82	20.90	26.78	205.48	64.75
G2010 Ave $E\%D$ (6 submissions*)			5.57	NA	-3.14	123.26	43.99
G2010 SD $E\%D$ (6 submissions*)			24.13	NA	15.63	142.49	60.75

* Averaged over KCS seakeeping cases reported in Chapter 4 with ($\lambda/L, Fr$) of (1.1, 0.26), (1.33, 0.26), and (2.00, 0.33)

Table 13- Average comparison error $|E|\%D$ for 0th harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	C_{T0}	AR	z_0/A	θ_0/Ak	Ave $ E \%D$
1	FORCE	StarCCM ⁺	2.43	8.85	13.01	144.31	42.15
2	HSVA	FreSCo ⁺	2.79	6.40	6.29	23.83	9.83
3	IIHR	CFDShip-Iowa V4.5	14.82	45.52	14.82	75.66	37.70
4	KRISO	WAVIS	7.69	22.08	24.37	627.38	170.38
5	MARIC	FINEMarine31_3	7.22	24.94	91.30	178.81	75.57
6	NMRI	NAGISA	11.02	53.75	6.95	123.08	48.70
7	NUMECA	ISISCFD	1.89	12.52	13.81	78.54	26.69
8	UDE	OpenFOAM	2.60	13.39	22.65	245.54	71.04
9	UM	OF23x	4.82	14.66	11.08	23.06	13.40
10	UNIZAG	swenseFoam	10.90	50.76	28.83	88.46	44.74
Ave $E \%D$			6.62	25.28	23.31	160.87	54.02
SD $E \%D$			4.25	17.10	23.73	168.49	53.39
G2010 Ave $E \%D$ (6 submissions*)			19.84	NA	11.44	152.08	61.12
G2010 SD $E \%D$ (6 submissions*)			14.83	NA	11.11	111.21	45.71

* Averaged over KCS seakeeping cases reported in Chapter 4 with ($\lambda/L, Fr$) of (1.1, 0.26), (1.33, 0.26), and (2.00, 0.33)

Table 14- Comparison error for 1st harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.65$

No	Institute	Code	ζ_1/L	$C_{T1} \times 10^3$		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.0051	3.348	-0.7121	0.1301	1.9065	0.0172	1.0984		
1	FORCE	StarCCM ⁺	-0.20	25.84	3.93	15.00	4.81	17.68	-0.22	14.68	2.99
2	HSVA	FreSCo ⁺	3.21	23.71	2.76	10.73	2.95	11.90	-0.35	12.39	2.02
3	IIHR	CFDShip-Iowa	0.29	9.72	4.68	-5.57	4.95	-19.49	7.31	8.77	5.65
4	KRISO	WAVIS	0.27	21.80	3.87	18.51	5.63	12.23	-1.35	13.20	3.62
5	MARIC	FINEMarine31_3		35.04		26.96		41.87		34.62	
6	NMRI	NAGISA	5.89	21.24	5.24	0.13	12.23	62.14	17.27	22.35	11.58
7	NUMECA	ISISCFD	-1.29	18.30	3.97	4.38	3.74	3.98	2.94	6.99	3.55
8	UDE	OpenFOAM		-9.88	5.00	-2.26	6.26			6.07	5.63
9	UM	OF23x	0.60	17.05	4.54	4.57	4.14	2.71	2.27	6.23	3.65
10	UNIZAG	swenseFoam		17.87	6.02	26.43	-33.30	176.09	2.79	73.46	14.04
Ave E%D			1.25	18.07	4.45	9.89	1.27	34.35	3.83	15.89	3.18
SD E%D			2.27	11.21	0.89	10.98	12.48	54.78	5.68	19.81	6.35
Ave E %D			1.68	20.04	4.45	11.45	8.67	38.68	4.31	17.96	5.81
SD E %D			1.98	7.09	0.89	9.34	9.07	51.82	5.32	17.56	5.09

Table 15- Comparison error for 1st harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.85$

No	Institute	Code	ζ_1/L	$C_{T1} \times 10^3$		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.0064	4.206	-1.2865	0.2438	0.9698	0.1462	1.3372		
1	FORCE	StarCCM ⁺									
2	HSVA	FreSCo ⁺	3.68	7.66	-10.99	4.53	-10.86	-50.99	-12.33	16.71	11.40
3	IIHR	CFDShip-Iowa	-0.24	-9.48	-11.94	-23.33	-7.35	-100.7	-11.22	33.44	10.17
4	KRISO	WAVIS	-0.14	6.74	-13.41	39.78	-21.07	-49.97	-11.91	24.16	15.46
5	MARIC	FINEMarine31_3		16.44		48.32		9.70		24.82	
6	NMRI	NAGISA	3.27	14.78	-6.80	18.09	-3.67	-38.53	-6.62	18.67	5.70
7	NUMECA	ISISCFD	-0.88	1.27	-11.21	5.11	-10.61	-59.50	-12.14	16.69	11.32
8	UDE	OpenFOAM	-0.24	-9.85	-3.46	11.82	-13.13	-50.50	-14.35	18.10	10.32
9	UM	OF23x	-0.37	4.90	-0.25	6.30	-9.76	-57.47	-6.81	17.26	5.61
10	UNIZAG	swenseFoam		12.24	-9.02	-4.20	-41.25	-44.58	-12.57	20.34	20.94
Ave E%D			0.73	4.97	-8.39	11.83	-14.71	-49.17	-10.99	16.67	11.36
SD E%D			1.76	9.03	4.27	20.48	11.07	26.74	2.61	14.50	5.98
Ave E %D			1.26	9.26	8.39	17.94	14.71	51.33	10.99	19.95	11.36
SD E %D			1.42	4.51	4.27	15.40	11.07	22.33	2.61	10.92	5.98

Table 16- Comparison error for 1st harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.15$

No	Institute	Code	ζ_1/L	$C_{T1} \times 10^3$		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.0101	3.929	-1.5459	0.8988	-3.101	0.7482	-2.495		
1	FORCE	StarCCM ⁺	-0.18			-9.96	4.27	4.57	5.83	4.90	5.05
2	HSVA	FreSCo ⁺	4.31			-7.13	1.61	-0.52	2.01	3.99	1.81
3	IIHR	CFDShip-Iowa	0.02	26.59	7.02	-9.11	0.93	-3.12	1.28	9.71	3.08
4	KRISO	WAVIS	-0.13			29.04	8.47	8.10	1.84	12.42	5.16
5	MARIC	FINEMarine31_3				11.77		28.09		19.93	
6	NMRI	NAGISA	5.86			-3.91	-3.41	8.15	-3.12	5.97	3.26
7	NUMECA	ISISCFD	0.00	17.44	-0.21	-4.28	0.27	-2.18	0.45	5.98	0.31
8	UDE	OpenFOAM	0.84			7.88	2.48			4.36	2.48
9	UM	OF23x	0.34			-2.16	2.00	-0.23	1.92	0.91	1.96
10	UNIZAG	swenseFoam		17.26	-5.54	-1.43	-13.66	8.69	2.09	9.13	7.10
Ave E%D			1.38	20.43	0.42	1.07	0.33	5.73	1.54	7.15	0.76
SD E%D			2.19	4.36	5.15	11.43	5.78	9.05	2.29	6.76	4.41
Ave E %D			1.46	20.43	4.26	8.67	4.12	7.07	2.32	9.41	3.57
SD E %D			2.14	4.36	2.93	7.52	4.07	8.04	1.50	5.52	2.83

Table 17- Comparison error for 1st harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.37$

No	Institute	Code	ζ_1/L	$C_{T1} \times 10^3$		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.0123	12.768	-1.3330	0.8745	-2.397	0.9655	-1.702		
1	FORCE	StarCCM ⁺	-0.07	5.97	2.38	-5.27	1.21	13.46	2.14	6.19	1.91
2	HSVA	FreSCo ⁺	4.24	12.34	-0.84	-4.30	9.83	-2.98	-0.81	5.97	3.83
3	IIHR	CFDShip-Iowa	0.16	7.72	-0.12	0.31	8.77	1.24	-1.03	2.36	3.31
4	KRISO	WAVIS	7.19	3.08	-6.80	10.44	4.39	8.26	-4.47	7.24	5.22
5	MARIC	FINEMarine31_3		51.65		-12.41		17.87		27.31	
6	NMRI	NAGISA	2.87	33.16	-3.89	16.98	13.41	23.25	-1.78	19.07	6.36
7	NUMECA	ISISCFD	-0.70	2.26	-1.16	-4.95	9.28	-4.87	-1.30	3.19	3.91
8	UDE	OpenFOAM									
9	UM	OF23x	-0.51	5.02	-0.72	-5.61	0.35	-3.40	2.33	3.64	1.13
10	UNIZAG	swenseFoam		13.56	-0.72	-5.24	11.71	2.20	-4.14	7.00	5.52
Ave E%D			1.88	14.97	-1.48	-1.12	7.37	6.11	-1.13	6.02	3.33
SD E%D			2.77	15.71	2.56	8.63	4.52	9.57	2.33	9.17	3.14
Ave E %D			2.25	14.97	2.08	7.28	7.37	8.61	2.25	8.28	3.90
SD E %D			2.49	15.71	2.11	4.77	4.52	7.39	1.29	7.59	2.64

Table 18- Comparison error for 1st harmonic of resistance and motions for KCS seakeeping submissions at $Fr=0.26$ and $\lambda/L=1.95$

No	Institute	Code	ζ_1/L	$C_{T1} \times 10^3$		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.0160	25.097	-0.6097	0.9331	-1.971	1.1194	-0.832		
1	FORCE	StarCCM ⁺	-0.56	10.98	-6.81	6.37	-5.38	3.13	-4.81	5.26	5.66
2	HSVA	FreSCo ⁺	0.10	8.01	-5.10	3.63	-5.06	2.91	-5.22	3.66	5.12
3	IIHR	CFDShip-Iowa	-0.75	5.59	-4.71	1.67	-4.85	2.58	-4.99	2.65	4.85
4	KRISO	WAVIS	-0.24	30.30	-6.48	20.55	-4.74	20.83	-5.51	17.98	5.58
5	MARIC	FINEMarine31_3		14.97		-1.17		-3.90		6.68	
6	NMRI	NAGISA	5.77	13.73	2.91	0.82	4.43	6.45	3.02	6.69	3.45
7	NUMECA	ISISCFD	-1.03	6.57	-5.46	3.81	-5.49	3.49	-5.52	3.72	5.49
8	UDE	OpenFOAM	-0.75	10.15	-6.22	-0.85	-5.97			3.92	6.09
9	UM	OF23x	0.00	7.77	-4.00	3.44	-3.66	3.68	-3.42	3.72	3.69
10	UNIZAG	swenseFoam		11.59	-5.13	6.10	6.73	7.23	-5.00	8.31	5.62
Ave E%D			0.32	11.97	-4.55	4.44	-2.66	5.16	-3.93	5.47	3.72
SD E%D			2.09	6.75	2.77	5.90	4.48	6.27	2.70	5.26	3.32
Ave E %D			1.15	11.97	5.20	4.84	5.15	6.02	4.68	6.00	5.01
SD E %D			1.78	6.75	1.17	5.58	0.84	5.45	0.88	4.89	0.96

Table 19- Average comparison error $E\%D$ for 1st harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	ζ_1/L	C_{T1}		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	Phase**	Amp	Phase	Amp	Phase	Amp	Phase
1	FORCE	StarCCM ⁺	-0.25	14.26	-0.16	1.54	1.23	9.71	0.74	6.44	0.71
2	HSVA	FreSCo ⁺	3.11	12.93	-3.54	1.49	-0.30	-7.94	-3.34	6.37	2.40
3	IIHR	CFDSHIP-Iowa	-0.10	8.03	-1.01	-7.21	0.49	-23.89	-1.73	9.81	1.08
4	KRISO	WAVIS	1.39	15.48	-5.71	23.66	-1.46	-0.11	-4.28	10.16	3.82
5	MARIC	FINEMarine31_3		29.53		14.69		18.73		20.98	
6	NMRI	NAGISA	4.73	20.73	-0.63	6.42	4.60	12.29	1.75	11.04	2.33
7	NUMECA	ISISCFD	-0.78	9.17	-2.81	0.81	-0.56	-11.82	-3.11	5.64	2.16
8	UDE	OpenFOAM	-0.05	-3.19	-1.56	4.15	-2.59	-50.50	-14.35	14.47	6.17
9	UM	OF23x	0.01	8.69	-0.11	1.31	-1.39	-10.94	-0.74	5.24	0.75
10	UNIZAG	swenseFoam		14.50	-2.88	4.33	-13.95	29.93	-3.37	16.25	6.73
Ave $E\%D$			1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
SD $E\%D$			1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
G2010 Ave $E\%D$ (6 submissions*)			NA	63.25	-17.09	3.16	-0.12	-1.33	-0.71	22.58	5.97
G2010 SD $E\%D$ (6 submissions*)			NA	28.90	30.29	12.22	1.61	5.51	4.85	15.54	12.25

Table 20- Average comparison error $|E|\%D$ for 1st harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	ζ_1/L	C_{T1}		z_1/A		θ_1/Ak		Ave.	
			Amp	Amp	Phase**	Amp	Phase	Amp	Phase	Amp	Phase
1	FORCE	StarCCM ⁺	1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
2	HSVA	FreSCo ⁺	1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
3	IIHR	CFDSHIP-Iowa	1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
4	KRISO	WAVIS	1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
5	MARIC	FINEMarine31_3	1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
6	NMRI	NAGISA	1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
7	NUMECA	ISISCFD	1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
8	UDE	OpenFOAM	1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
9	UM	OF23x	1.01	13.01	-2.05	5.12	-1.55	-3.46	-3.16	5.65	2.25
10	UNIZAG	swenseFoam	1.82	8.14	1.75	8.06	4.80	21.95	4.39	9.99	3.65
Ave $ E \%D$			1.47	14.71	4.92	9.83	7.75	24.34	5.71	12.59	6.13
SD $ E \%D$			1.53	5.98	1.30	6.28	5.03	13.47	3.19	6.82	3.17
G2010 Ave $ E \%D$ (6 sub.*)			NA	63.25	18.13	9.43	1.28	4.06	4.48	25.58	7.96
G2010 SD $ E \%D$ (6 sub.*)			NA	28.90	29.68	8.39	0.99	3.96	1.99	13.75	10.89

* Averaged over KCS seakeeping cases reported in Chapter 4 with ($\lambda/L, Fr$) of (1.1, 0.26), (1.33, 0.26), and (2.00, 0.33)

**Phase error is normalized by 2π ($E\%2\pi = 100 \times (D - S)/2\pi$)

Table 21- Comparison error for 2nd harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.65$

No	Institute	Code	$C_{T2} \times 10^3$		z_2/A		θ_2/Ak		Ave.	
			Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.652	0.0678	0.0052	-0.0463	0.0012	0.6052		
1	FORCE	StarCCM ⁺	68.17	7.37	91.33	-37.56	32.54	-26.96	64.01	23.96
2	HSVA	FreSCo ⁺	70.89	4.11	88.83	-47.87	29.89	-30.06	63.20	27.35
3	IIHR	CFDShip-Iowa	56.52	7.99	76.16	-31.53	22.34	-27.44	51.67	22.32
4	KRISO	WAVIS	64.95	7.84	79.87	-38.40	24.97	-27.13	56.60	24.45
5	MARIC	FINEMarine31_3	68.40		3.55		-317.68		129.88	
6	NMRI	NAGISA	26.37	9.76	-42.74	-40.68	8.11	-23.48	25.74	24.64
7	NUMECA	ISISCFD	63.12	6.46	-39.07	-38.95	-180.51	-24.86	94.23	23.42
8	UDE	OpenFOAM	16.70	1.83					16.70	1.83
9	UM	OF23x	66.59	9.62	87.86	-46.93	12.40	-29.93	55.62	28.83
10	UNIZAG	swenseFoam	59.23	35.53	86.48	18.53	37.13	-2.84	60.95	18.97
Ave E%D			56.09	10.06	48.03	-32.92	-36.76	-24.09	46.96	22.36
SD E%D			17.89	9.32	53.97	20.05	118.33	8.30	63.40	12.56
Ave E %D			56.09	10.06	66.21	37.55	73.95	24.09	65.42	23.90
SD E %D			17.89	9.32	28.91	8.70	99.42	8.30	48.74	8.77

Table 22- Comparison error for 2nd harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=0.85$

No	Institute	Code	$C_{T2} \times 10^3$		z_2/A		θ_2/Ak		Ave.	
			Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.755	-1.1217	0.0082	0.8105	0.0022	1.2154		
1	FORCE	StarCCM ⁺								
2	HSVA	FreSCo ⁺	40.08	27.62	41.83	-46.34	-6.45	-43.84	29.45	39.26
3	IIHR	CFDShip-Iowa	4.00	-16.90	-6.51	-42.93	-88.87	-34.04	33.13	31.29
4	KRISO	WAVIS	34.46	-16.64	40.03	-41.87	21.14	-39.96	31.88	32.82
5	MARIC	FINEMarine31_3	49.16		-57.61		-353.91		153.56	
6	NMRI	NAGISA	-8.44	-17.14	9.07	-32.06	-117.88	-35.38	45.13	28.19
7	NUMECA	ISISCFD	31.34	-21.23	14.19	-46.64	-55.19	-42.57	33.57	36.81
8	UDE	OpenFOAM	12.88	-28.95					12.88	28.95
9	UM	OF23x	38.89	3.22	41.50	-42.93	2.98	-30.31	27.79	25.49
10	UNIZAG	swenseFoam	21.17	23.02	40.36	46.11	-1.92	1.74	21.15	23.62
Ave E%D			24.84	-5.88	15.36	-29.52	-75.01	-32.05	38.40	22.48
SD E%D			17.81	19.91	32.52	31.20	114.88	14.50	55.07	21.87
Ave E %D			26.71	19.34	31.39	42.70	81.04	32.55	46.38	31.53
SD E %D			14.85	7.55	17.56	4.70	110.71	13.35	47.71	8.53

Table 23- Comparison error for 2nd harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.15$

No	Institute	Code	$C_{T2} \times 10^3$		z_2/A		θ_2/Ak		Ave.	
			Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	2.697	1.8294	0.0128	0.2139	0.0139	0.2010		
1	FORCE	StarCCM ⁺			-35.61	8.50	24.95	14.84	30.28	11.67
2	HSVA	FreSCo ⁺			-2.92	2.02	7.06	2.14	4.99	2.08
3	IIHR	CFDShip-Iowa	-29.87	11.42	20.50	2.62	9.36	5.76	19.91	6.60
4	KRISO	WAVIS			14.09	7.50	-6.35	12.96	10.22	10.23
5	MARIC	FINEMarine31_3			-64.31		-22.74		43.53	
6	NMRI	NAGISA			-112.04	-3.27	-24.90	-16.38	68.47	9.83
7	NUMECA	ISISCFD	17.57	1.06	-2.42	1.72	5.14	1.11	8.38	1.30
8	UDE	OpenFOAM								
9	UM	OF23x			-0.57	2.06	12.67	3.35	6.62	2.71
10	UNIZAG	swenseFoam	25.29	-38.91	30.38	29.54	6.68	-34.96	20.78	34.47
Ave E%D			4.33	-8.81	-16.99	6.34	1.32	-1.40	7.55	5.52
SD E%D			24.39	21.70	43.35	9.41	15.47	15.46	27.74	15.53
Ave E %D			24.24	17.13	31.43	7.15	13.32	11.44	23.00	11.91
SD E %D			5.08	15.97	34.36	8.81	7.98	10.50	15.80	11.76

Table 24- Comparison error for 2nd harmonic of resistance and motions for KCS seakeeping submissions at Fr=0.26 and $\lambda/L=1.37$

No	Institute	Code	$C_{T2} \times 10^3$		z_2/A		θ_2/Ak		Ave.	
			Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	2.201	2.9030	0.0068	0.5799	0.0118	0.7084		
1	FORCE	StarCCM ⁺	5.45	103.35	-21.93	4.38	1.18	3.11	9.52	36.95
2	HSVA	FreSCo ⁺	18.04	-0.73	12.52	-140.92	13.48	0.75	14.68	47.47
3	IIHR	CFDShip-Iowa	-67.69	3.39	-34.67	-145.53	-2.43	2.08	34.93	50.33
4	KRISO	WAVIS	35.71	-8.61	22.84	-424.82	-63.40	-6.66	40.65	146.7
5	MARIC	FINEMarine31_3	-29.32		-12926		-220.87		4392.22	
6	NMRI	NAGISA	67.16	-1.69	10.72	-446.37	53.56	-6.45	43.81	151.5 0
7	NUMECA	ISISCFD	2.98	-3.33	-3.23	-109.99	-11.32	0.04	5.85	37.79
8	UDE	OpenFOAM								
9	UM	OF23x	8.37	-0.68	-4.90	37.03	-14.92	7.67	9.40	15.13
10	UNIZAG	swenseFoam	11.37	-35.96	-41.32	435.04	-9.79	10.35	20.83	160.4
Ave E%D			5.79	6.97	-1443	-98.90	-28.28	1.36	492.33	35.74
SD E%D			35.73	38.22	4060.10	261.07	73.87	5.61	1389.90	101.6
Ave E %D			27.34	19.72	1453.18	218.01	43.44	4.64	507.99	80.79
SD E %D			23.71	33.48	4056.44	174.38	66.10	3.43	1382.09	70.43

Table 25- Comparison error for 2nd harmonic of resistance and motions for KCS seakeeping submissions at $Fr=0.26$ and $\lambda/L=1.95$

No	Institute	Code	$C_{T2} \times 10^3$		z_2/A		θ_2/Ak		Ave.	
			Amp	ε [rad]	Amp	ε [rad]	Amp	ε [rad]	Amp	Phase
	FORCE	Experiment	0.675	-0.4461	0.0204	0.7941	0.0372	1.6463		
1	FORCE	StarCCM ⁺	38.32	7.28	16.29	-7.70	12.29	-6.88	22.30	7.29
2	HSVA	FreSCo ⁺	1.68	-6.39	10.91	-11.29	-3.91	-10.66	5.50	9.45
3	IIHR	CFDShip-Iowa	-159.26	21.99	8.60	-9.16	-8.61	-8.89	58.82	13.35
4	KRISO	WAVIS	0.75	33.85	-1.07	-1.43	54.28	16.46	18.70	17.25
5	MARIC	FINEMarine31_3	-64.05		-2.72		-4.95		23.91	
6	NMRI	NAGISA	-41.40	11.58	31.52	1.03	-30.78	10.34	34.57	7.65
7	NUMECA	ISISCFD	8.29	-5.59	7.20	-11.13	1.39	-10.44	5.63	9.05
8	UDE	OpenFOAM	-133.05	-3.52					133.05	3.52
9	UM	OF23x	0.42	-0.95	8.83	-5.95	1.99	-6.79	3.75	4.56
10	UNIZAG	swenseFoam	27.84	-26.47	3.64	100.14	2.13	-36.40	11.20	54.34
Ave E%D			-32.05	3.53	9.24	6.81	2.65	-6.66	14.65	5.67
SD E%D			63.97	16.64	9.63	35.51	21.36	14.76	31.65	22.30
Ave E %D			47.51	13.07	10.09	18.48	13.37	13.36	23.65	14.97
SD E %D			53.51	10.88	8.74	31.08	16.87	9.16	26.37	17.04

Table 26- Average comparison error $E\%D$ for 2nd harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	C _T		Heave		Pitch		Ave.	
			Amp	Phase**	Amp	Phase	Amp	Phase	Amp	Phase
1	FORCE	StarCCM ⁺	37.31	39.33	12.52	-8.09	17.74	-3.97	22.52	17.13
2	HSVA	FreSCo ⁺	32.67	6.15	30.24	-48.88	8.02	-16.33	23.64	23.79
3	IIHR	CFDShip-Iowa	-39.26	5.58	12.82	-45.31	-13.64	-12.51	21.91	21.13
4	KRISO	WAVIS	33.97	4.11	31.15	-99.80	6.13	-8.86	23.75	37.59
5	MARIC	FINEMarine31_3	6.05		-2609.51		-184.0		933.20	
6	NMRI	NAGISA	10.92	0.63	-20.69	-104.27	-22.38	-14.27	18.00	39.72
7	NUMECA	ISISCFD	24.66	-4.53	-4.67	-41.00	-48.10	-15.34	25.81	20.29
8	UDE	OpenFOAM	-34.49	-10.21					34.49	10.21
9	UM	OF23x	28.57	2.80	26.54	-11.35	3.02	-11.20	19.38	8.45
10	UNIZAG	swenseFoam	28.98	-8.56	23.91	125.87	6.85	-12.42	19.91	48.95
Ave E%D			12.94	3.92	-277.52	-29.10	-25.16	-11.86	105.21	14.96
SD E%D			26.63	13.75	824.64	67.28	59.30	3.71	303.52	28.25
G2010 Ave E%D (6 submissions*)			NA	NA	NA	NA	NA	NA	NA	NA
G2010 SD E%D (6 submissions*)			NA	NA	NA	NA	NA	NA	NA	NA

Table 27- Average comparison error $|E|\%D$ for 2nd harmonic of resistance and motions over five wavelength conditions ($\lambda/L=0.65, 0.85, 1.15, 1.37, 1.95$) for KCS seakeeping submissions at $Fr=0.26$

No	Institute	Code	C _T		Heave		Pitch		Ave.	
			Amp	Phase**	Amp	Phase	Amp	Phase	Amp	Phase
1	FORCE	StarCCM ⁺	37.31	39.33	41.29	14.54	17.74	12.95	32.11	22.27
2	HSVA	FreSCo ⁺	32.67	9.71	31.40	49.69	12.16	17.49	25.41	25.63
3	IIHR	CFDShip-Iowa	63.47	12.34	29.29	46.35	26.32	15.64	39.69	24.78
4	KRISO	WAVIS	33.97	16.74	31.58	102.80	34.03	20.63	33.19	46.72
5	MARIC	FINEMarine31_3	52.73		2610.94		184.03		949.23	
6	NMRI	NAGISA	35.84	10.04	41.22	104.68	47.05	18.40	41.37	44.38
7	NUMECA	ISISCFD	24.66	7.53	13.22	41.69	50.71	15.80	29.53	21.67
8	UDE	OpenFOAM	54.21	11.43					54.21	11.43
9	UM	OF23x	28.57	3.62	28.73	26.98	8.99	15.61	22.10	15.40
10	UNIZAG	swenseFoam	28.98	31.98	40.44	125.87	11.53	17.26	26.98	58.37
Ave $ E \%D$			39.24	15.86	318.68	64.08	43.62	16.72	133.85	32.22
SD $ E \%D$			12.29	11.23	810.48	38.44	51.70	2.14	291.49	17.27
G2010 Ave $ E \%D$ (6 submissions*)			NA	NA	NA	NA	NA	NA	NA	NA
G2010 SD $ E \%D$ (6 submissions*)			NA	NA	NA	NA	NA	NA	NA	NA

* Averaged over KCS seakeeping cases reported in Chapter 4 with ($\lambda/L, Fr$) of (1.1, 0.26), (1.33, 0.26), and (2.00, 0.33)

**Phase error is normalized by 2π ($E\%2\pi = 100 \times (D - S)/2\pi$)